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STATISTICS & PROBABILITY

for Senior High School

Revised Edition

Christian Paul O. Chan Shio
Maria Angeli T. Reyes

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